

LAMPIRAN



Lampiran 1

Data Tegangan Sekunder Koil Tesla

- I. Tegangan sumber, Vdc = 9.01 Volt
 Jumlah lilitan primer, Np = 460
 Time/div. = 50 micro-Second
 Volt/div. = 5 mili-Volt

Jumlah lilitan sekunder, Ns	Tegangan primer Vp (mV)	Tegangan sekunder, Vs (mV)				
		R1 = 4,5 cm	R2 = 5,5 cm	R3 = 6,5 cm	R4 = 7,5 cm	R5 = 8,5 cm
704	5	4	3	2	2	1
875		6	4	3	3	1.5
958		7	5	4	3	2
1125		8	6	5	4	2.5
1208		9	6	5	4	2.5

- II. Tegangan sumber, Vdc = 9.01 Volt
 Jumlah lilitan primer, Np = 920
 Time/div. = 5 micro-Second
 Volt/div. = 10 mili-Volt

Jumlah lilitan sekunder, Ns	Tegangan primer Vp (mV)	Tegangan sekunder, Vs (mV)				
		R1 = 4,5 cm	R2 = 5,5 cm	R3 = 6,5 cm	R4 = 7,5 cm	R5 = 8,5 cm
704	16	8	4	4	3	2
875		10	6	5	4	3
958		13	7	6	4	4
1125		18	12	8	7	5
1208		18	12	8	7	5

- III. Tegangan sumber, Vdc = 13.23 Volt
 Jumlah lilitan primer, Np = 460
 Time/div. = 50 micro-Second
 Volt/div. = 5 mili-Volt

Jumlah lilitan sekunder, Ns	Tegangan primer Vp (mV)	Tegangan sekunder, Vs (mV)				
		R1 = 4,5 cm	R2 = 5,5 cm	R3 = 6,5 cm	R4 = 7,5 cm	R5 = 8,5 cm
704	10	9	5	4	3	2
875		13	7	6	4	2.5
958		15	9	7	5	3
1125		18	12.5	9	6	5
1208		19	12.5	9	6	5

IV. Tegangan sumber, V_{dc} = 13.23 Volt
 Jumlah lilitan primer, N_p = 920
 Time/div. = 5 micro-Second
 Volt/div. = 20 mili-Volt

Jumlah lilitan sekunder, N_s	Tegangan primer V_p (mV)	Tegangan sekunder, V_s (mV)				
		$R1 = 4,5 \text{ cm}$	$R2 = 5,5 \text{ cm}$	$R3 = 6,5 \text{ cm}$	$R4 = 7,5 \text{ cm}$	$R5 = 8,5 \text{ cm}$
704	36	14	8	8	6	4
875		20	12	10	8	6
959		24	16	12	10	8
1125		36	24	18	16	10
1208		36	24	18	16	10



Lampiran 2.

Spesifikasi Fisis Koil Tesla

Spesifikasi	Sirkuit Primer	Sirkuit Sekunder
Diamater kumparan	3,2 cm	4,3 cm
Radius kawat	0,15 mm	0,4 mm
Panjang kumparan	6,9 cm	6,3 cm
Jumlah lilitan	460	959 dobel
Induktansi	644,3 mikro-Henry	6,96 mili-Henry
Frekuensi terukur	1,9 KHz	1,9 KHz
Resistansi kumparan	8,2 Ohm	5,56 Ohm
Kapasitansi	39,3 mikro-Farad	3,63 nano-Farad



Karakteristik Elektrik DC $T_A = 25^\circ\text{C}$, $V_{CC} = +5 - +15\text{ V}$ kecuali kalau dinyatakan lain.

PARAMETER	TEST CONDITIONS	SE555			NE555/SE555C			UNIT
		Min	Typ	Max	Min	Typ	Max	
Supply voltage		4.5		18	4.5		16	V
Supply current (low state) ¹	$V_{CC} = 5\text{V } R_L = \infty$ $V_{CC} = 15\text{V } R_L = \infty$		3 10	5 12		3 10	6 15	 mA
Timing error (monostable) Initial accuracy ² Drift with temperature Drift with supply voltage	$R_A = 2\text{k}\Omega$ to $100\text{k}\Omega$ $C = 0.1\mu\text{F}$		0.5 30 0.05	2.0 100 0.2		1.0 50 0.1	3.0 150 0.5	 % ppm/ $^\circ\text{C}$ %/V
Timing error (astable) Initial accuracy ² Drift with temperature Drift with supply voltage	$R_A, R_B = 1\text{k}\Omega$ to $100\text{k}\Omega$ $C = 0.1\mu\text{F}$ $V_{CC} = 15\text{V}$		1.5 90 0.15			2.25 150 0.3		 % ppm/ $^\circ\text{C}$ %/V
Control voltage level	$V_{CC} = 15\text{V}$	9.6	10.0	10.4	9.0	10.0	11.0	V
Threshold voltage	$V_{CC} = 5\text{V}$ $V_{CC} = 15\text{V}$ $V_{CC} = 5\text{V}$	2.9 9.4 2.7	3.33 10.0 3.33	3.8 10.6 4.0	2.6 8.8 2.4	3.33 10.0 3.33	4.0 11.2 4.2	 V V V
Threshold current ³			0.1	0.25		0.1	0.25	μA
Trigger voltage	$V_{CC} = 15\text{V}$ $V_{CC} = 5\text{V}$	4.8 1.45	5.0 1.67	5.2 1.9	4.5 1.1	5.0 1.67	5.6 2.2	 V V
Trigger current	$V_{TRIG} = 0\text{V}$		0.5	0.9		0.5	2.0	μA
Reset voltage ⁴		0.4	0.7	1.0	0.4	0.7	1.0	V
Reset current			0.1	0.4		0.1	0.4	μA
Reset current	$V_{RESET} = 0\text{V}$		0.4	1.0		0.4	1.5	μA
Output voltage (low)	$V_{CC} = 15\text{V}$ $I_{SINK} = 10\text{mA}$ $I_{SINK} = 50\text{mA}$ $I_{SINK} = 100\text{mA}$ $I_{SINK} = 200\text{mA}$ $V_{CC} = 5\text{V}$ $I_{SINK} = 8\text{mA}$ $I_{SINK} = 5\text{mA}$		0.1 0.4 2.0 2.5	0.15 0.5 2.2		0.1 0.4 2.0 2.5	0.25 0.75 2.5	 V V V V V V V V
Output voltage (high)	$V_{CC} = 15\text{V}$ $I_{SOURCE} = 200\text{mA}$ $I_{SOURCE} = 100\text{mA}$ $V_{CC} = 5\text{V}$ $I_{SOURCE} = 100\text{mA}$		12.5 13.0 3.0			12.5 13.3 3.3		 V V V
Turn off times	$V_{RESET} = V_{CC}$		0.5	2.0		0.5		μs
Rise time of output			100	200		100	300	ns
Fall time of output			100	200		100	300	ns
Discharge leakage current			20	100		20	100	na

CATATAN

1. Arus catu bila keluaran tinggi, lumrahnya 1 mA atau kurang
2. Diuji pada $V_{CC} = 5\text{V}$ dan $V_{CC} = 15\text{V}$
3. Ini akan menentukan harga maksimum $R_A + R_B$, untuk pengoperasian pada 15 V, total maksimum $R = 10\text{ M}\Omega$, untuk pengoperasian pada 5 V, total maks. $R = 3,4\text{ M}\Omega$
4. Ditentukan dengan masukan sulut tinggi
5. Waktu terukur dari denyut mengarah ke positif dari 0 hingga $0,8 \times V_{CC}$ ke ambang, sampai keluaran jatuh dari tinggi ke rendah.

Penerapan

Monostabil:
 $t \approx 1,1 \times R_A \times C$

Takstabil:

$$t_1 \approx 0,7 \times (R_A + R_B) \times C$$

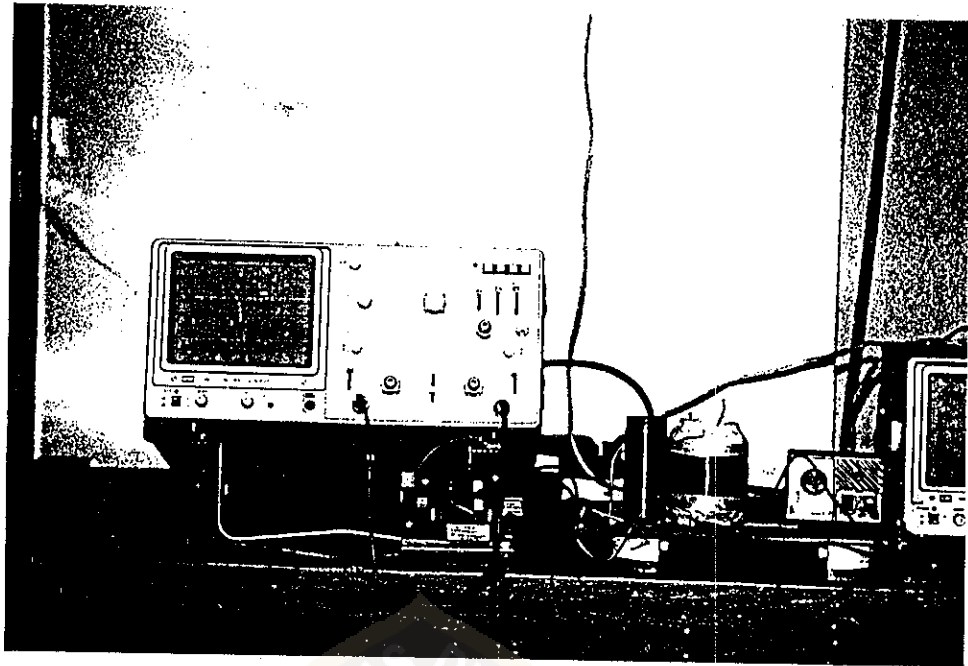
$$t_2 \approx 0,7 \times R_B \times C$$

$$T = t_1 + t_2$$

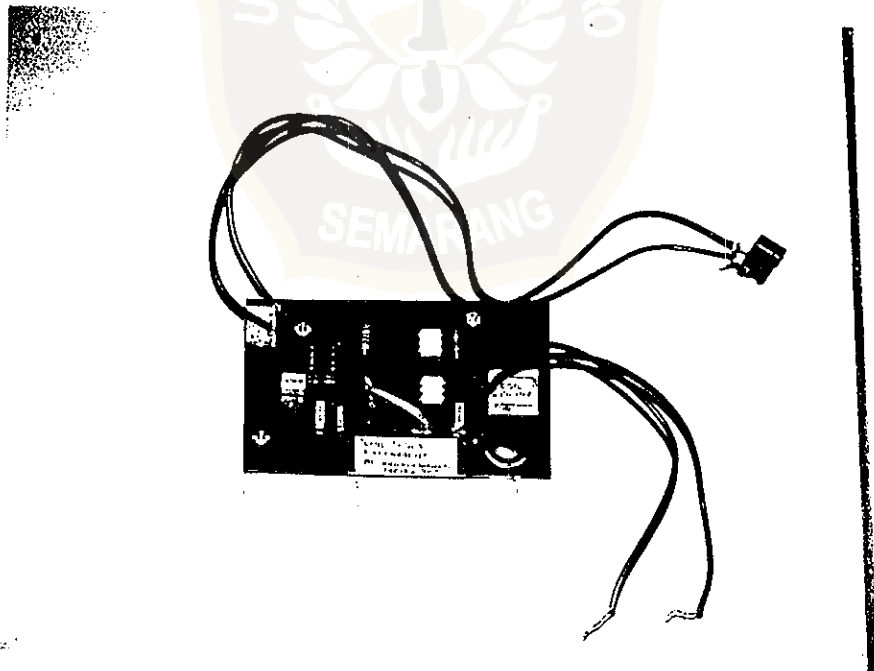
- Pewaktuan (*timing*) dengan cermat
- Pembangkit denyut
- Pewaktuan sekuensi
- Pembangkitan tundaan waktu
- Pemodulasian lebar denyut
- Pemodulasian posisi denyut
- Detektor denyut hilang

Lampiran 3

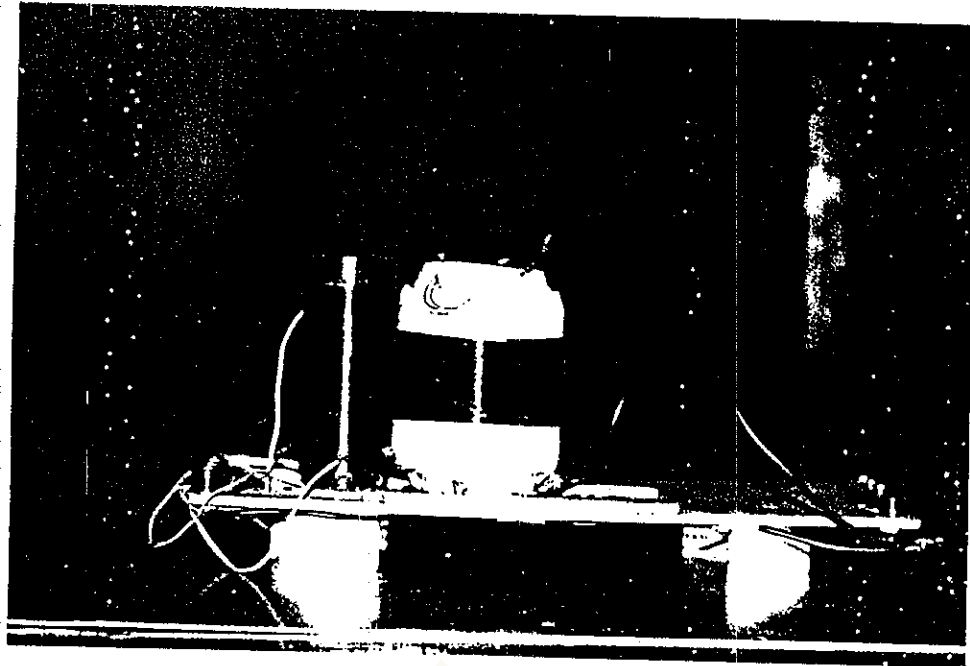
Foto Alat-alat Percobaan



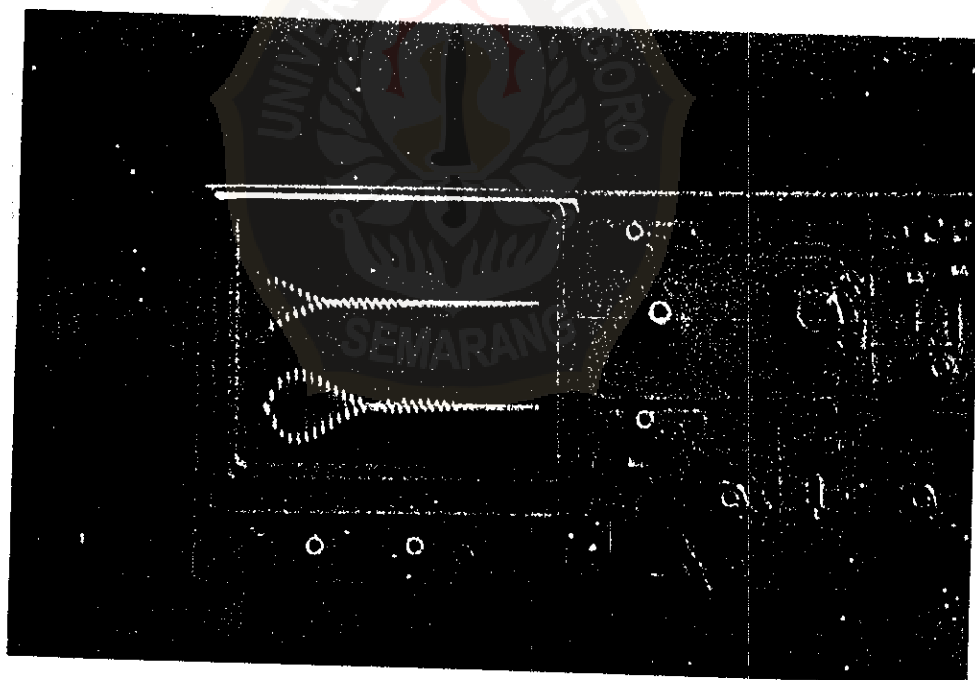
3.1. Alat Percobaan Simulasi Koil Tesla



3.2. Rangkaian Pembangkit Gelombang Persegi dan MOC 3011



3.3. Koil Tesla



3.4. Osiloskop dan grafik transfer energi hasil percobaan

NE/SE 555 Pewaktu (Timer)

Penjelasan Umum

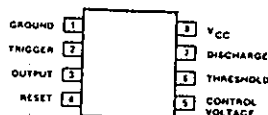
Rangkaian pewaktu monolit NE/SE 555 adalah pengatur yang mantap yang mampu membangkitkan tundaan waktu atau pun guncangan yang cermat. Ada terminal-terminal tambahan guna penyulutan atau pengondisian ulang (*reset*), kalau diinginkan.

Dalam ragam operasi tundaan waktu, waktu dikendalikan dengan teliti dengan sebuah resistor dan kondensator ekstern. Untuk beroperasi takmantap sebagai osilator, frekuensi bebas, dan daur aktif (*duty cycle*) dikendalikan dengan teliti oleh dua resistor dan satu kondensator ekstern.

Rangkaiannya akan dapat disulut dan di-*reset* pada bentuk gelombang yang sedang jatuh, dan susunan keluarannya akan dapat merupakan sumber ataupun benaman (*sink*) sampai 200 mA ataupun dapat menggerakkan rangkaian-rangkaian TTL.

RC 555 dapat beroperasi dalam jelajahan suhu dari 0° C hingga +70° C. RM 555 tahan terhadap suhu lebih tinggi, dan beroperasi dalam -55° C hingga +125° C.

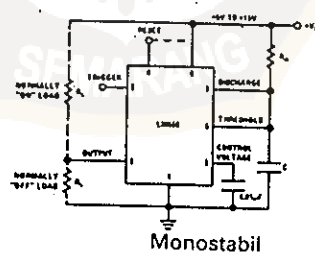
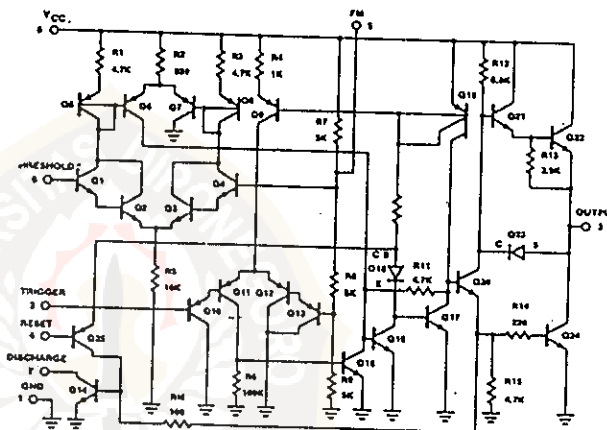
Diagram koneksi



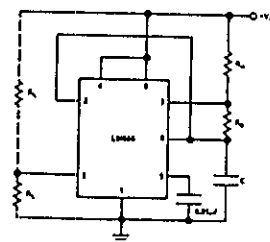
Tarif Maksimum Mutlak

Parameter	Tarif	Satuan
Tegangan catu SE555	+18	V
NE555, SE555C	+16	V
Borosan daya	600	mW
Jelajahan suhu operasi NE555	0 s/d +70	°C
SE555, SE555C	-55 s/d +125	°C
Jelajahan suhu simpan	-65 s/d +150	°C
Suhu timah (penyolderan 60 detik)	300	°C

Skema



Monostabil



Takstabil

Sifat-sifat

- Waktu mati (*off*) kurang dari 12 μ det
- Frekuensi operasi tertinggi besar dari 500 kHz
- Pewaktuan (*timing*) dari mikrodetik hingga jam
- Beroperasi dalam ragam takstabil dan monostab
- Arus keluaran tinggi
- Daure aktif (*duty cycl.*) dapat distel
- Serba-cocok dengan TI
- Kemantapan suhu 0,005 per °C

MOC3010 MOC3011 MOC3012

ELECTRICAL CHARACTERISTICS ($T_A = 25^\circ\text{C}$ unless otherwise noted)

Characteristic	Symbol	Min	Typ	Max	Unit
INPUT LED					
Reverse Leakage Current ($V_R = 3\text{ V}$)	I_R	—	0.05	100	μA
Forward Voltage ($I_F = 10\text{ mA}$)	V_F	—	1.15	1.5	Volts
OUTPUT DETECTOR ($I_F = 0$ unless otherwise noted)					
Peak Blocking Current, Either Direction (Rated $V_{DRM}^{(1)}$)	I_{DRM}	—	10	100	nA
Peak On-State Voltage, Either Direction ($I_{TM} = 100\text{ mA Peak}$)	V_{TM}	—	1.8	3	Volts
Critical Rate of Rise of Off-State Voltage (Figure 7, Note 2)	dv/dt	—	10	—	$\text{V}/\mu\text{s}$
COUPLED					
LED Trigger Current, Current Required to Latch Output (Main Terminal Voltage = 3 V(3))	I_{FT}	—	8 5 3	15 10 5	mA
Holding Current, Either Direction	I_H	—	100	—	μA

1. Test voltage must be applied within dv/dt rating.
2. This is static dv/dt . See Figure 7 for test circuit. Commutating dv/dt is a function of the load-driving thyristor(s) only.
3. All devices are guaranteed to trigger at an I_F value less than or equal to max I_{FT} . Therefore, recommended operating I_F lies between max I_{FT} (15 mA for MOC3010, 10 mA for MOC3011, 5 mA for MOC3012) and absolute max I_F (60 mA).

TYPICAL ELECTRICAL CHARACTERISTICS $T_A = 25^\circ\text{C}$

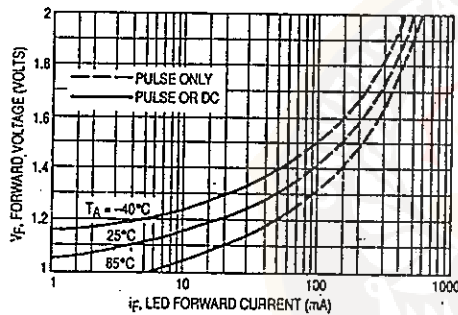


Figure 1. LED Forward Voltage versus Forward Current

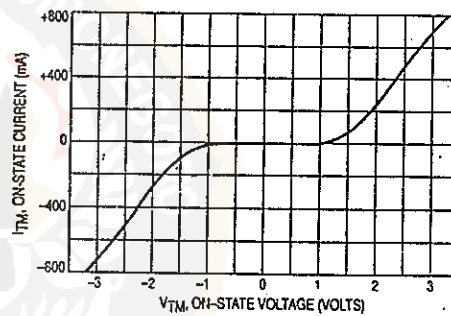


Figure 2. On-State Characteristics

MOTOROLA
 SEMICONDUCTOR TECHNICAL DATA

**6-Pin DIP Random-Phase
 Optoisolators Triac Driver Output
 (250 Volts Peak)**

The MOC3010 Series consists of gallium arsenide infrared emitting diodes, optically coupled to silicon bilateral switch and are designed for applications requiring isolated triac triggering, low-current isolated ac switching, high electrical isolation (to 7500 Vac peak), high detector standoff voltage, small size, and low cost.

- To order devices that are tested and marked per VDE 0884 requirements, the suffix "V" must be included at end of part number. VDE 0884 is a test option.

Recommended for 115 Vac(rms) Applications:

- Solenoid/Valve Controls
- Lamp Ballasts
- Interfacing Microprocessors to 115 Vac Peripherals
- Motor Controls
- Static ac Power Switch
- Solid State Relays
- Incandescent Lamp Dimmers

MAXIMUM RATINGS ($T_A = 25^\circ\text{C}$ unless otherwise noted)

Rating	Symbol	Value	Unit
--------	--------	-------	------

INFRARED EMITTING DIODE

Reverse Voltage	V_R	3	Volts
Forward Current — Continuous	I_F	60	mA
Total Power Dissipation @ $T_A = 25^\circ\text{C}$ Negligible Power in Transistor Derate above 25°C	P_D	100 1.33	mW mW/°C

OUTPUT DRIVER

Off-State Output Terminal Voltage	V_{ORM}	250	Volts
Peak Repetitive Surge Current ($P_W = 1 \text{ ms}$, 120 pps)	I_{TSM}	1	A
Total Power Dissipation @ $T_A = 25^\circ\text{C}$ Derate above 25°C	P_D	300 4	mW mW/°C

TOTAL DEVICE

Isolation Surge Voltage(1) (Peak ac Voltage, 60 Hz, 1 Second Duration)	V_{ISO}	7500	Vac(pk)
Total Power Dissipation @ $T_A = 25^\circ\text{C}$ Derate above 25°C	P_D	330 4.4	mW mW/°C
Junction Temperature Range	T_J	-40 to +100	°C
Ambient Operating Temperature Range(2)	T_A	-40 to +85	°C
Storage Temperature Range(2)	T_{stg}	-40 to +150	°C
Soldering Temperature (10 s)	T_L	260	°C

- Isolation surge voltage, V_{ISO} , is an internal device dielectric breakdown rating. For this test, Pins 1 and 2 are common, and Pins 4, 5 and 6 are common.
- Refer to Quality and Reliability Section in Opto Data Book for information on test conditions. Preferred devices are Motorola recommended choices for future use and best overall value.

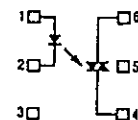
(Replaces MOC3009/D)

MOC3010
 [IFT = 15 mA Max]
MOC3011
 [IFT = 10 mA Max]
MOC3012*
 [IFT = 5 mA Max]

*Motorola Preferred Device

STYLE 6 PLASTIC


STANDARD THRU HOLE
 CASE 730A-04

COUPLER SCHEMATIC


- ANODE
- CATHODE
- NC
- MAIN TERMINAL
- SUBSTRATE
DO NOT CONNECT
- MAIN TERMINAL

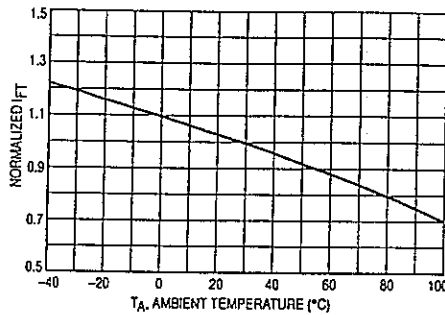


Figure 3. Trigger Current versus Temperature

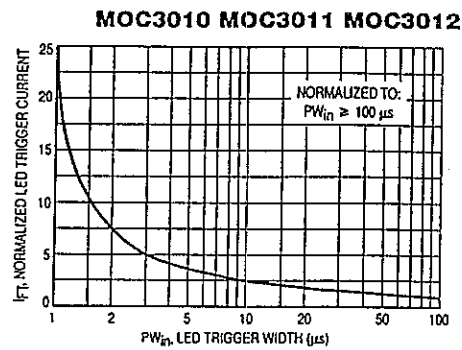


Figure 4. LED Current Required to Trigger versus LED Pulse Width

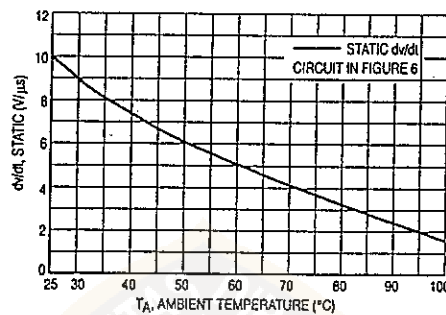
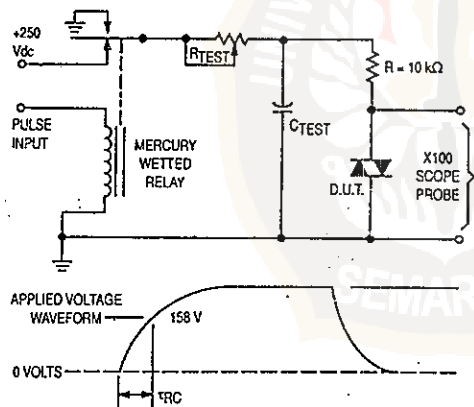


Figure 5. dv/dt versus Temperature



1. The mercury wetted relay provides a high speed repeated pulse to the D.U.T.
2. 100x scope probes are used, to allow high speeds and voltages.
3. The worst-case condition for static dv/dt is established by triggering the D.U.T. with a normal LED input current, then removing the current. The variable R_{TEST} allows the dv/dt to be gradually increased until the D.U.T. continues to trigger in response to this applied voltage pulse, even after the LED current has been removed. The dv/dt is then decreased until the D.U.T. stops triggering. τ_{RC} is measured at this point and recorded.

$$\frac{dv}{dt} = \frac{0.63 V_{max}}{\tau_{RC}} = \frac{158}{\tau_{RC}}$$

Figure 6. Static dv/dt Test Circuit

International **IR** Rectifier BOSFET® Photovoltaic Relay

PD 1.028C

Series PVR33

Microelectronic

Power IC Relay

Dual-Pole, 400mA, 0-100V AC/DC

General Description

The PVR33 Photovoltaic Relay is a dual-pole, normally open solid state replacement for electro-mechanical relays. It utilizes as an output switch a unique bidirectional (AC or DC) MOSFET power IC termed a BOSFET. The BOSFET is controlled by a photovoltaic generator of novel construction, which is energized by radiation from a dielectrically isolated light emitting diode (LED).

The PVR overcomes the limitations of reed relays by offering the solid state advantages of long life, high operating speed, low pick-up power, bounce-free operation, low thermal voltages and miniaturization. These advantages allow product improvement and design innovations in many applications such as process control, multiplexing, telecommunications, automatic test equipment and data acquisition.

The PVR can switch analog signals from thermocouple level to 300 volts peak AC or DC polarity. Signal frequencies into the RF range are easily controlled and switching rates up to 5kHz are achievable. The extremely small thermally generated offset voltages allow increased measurement accuracies.

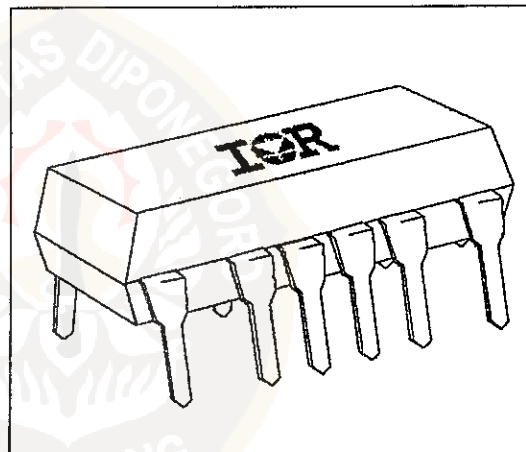
Unique silicon technology developed by International Rectifier forms the heart of the PVR. The monolithic BOSFET contains a bidirectional N-channel power MOSFET output structure. In addition, this power IC chip has input circuitry for fast turn-off and gate protection functions. This section of the BOSFET chip utilizes both bipolar and MOS technology to form NPN transistors, P-channel MOSFETs, resistors, diodes and capacitors.

The photovoltaic generator similarly utilizes a unique International Rectifier alloyed multijunction structure. The excellent current conversion efficiency of this technique results in the very fast response of the PVR microelectronic power IC relay.

This advanced semiconductor technology has created a radically new control device. Designers can now develop switching systems to new standards of electrical performance and mechanical compactness.

PVR33 Features

- BOSFET Power IC ■
- 10¹⁰ Operations ■
- 100µsec Operating Time ■
- 0.2µV Thermal Offset ■
- 5 milliwatts Pick-Up Power ■
- 1000V/µsec dv/dt ■
- Bounce-Free ■
- 16-pin DIP Package ■
- 40°C to 85°C ■

**Part Identification**

Part Number	Operating Voltage (AC/DC)	Off-State Resistance
PVR2300	0 – 200V	10 ⁸ Ohms
PVR3300	0 – 300V	10 ⁸ Ohms
PVR3301	0 – 300V	10 ¹⁰ Ohms

(BOSFET is a trademark of International Rectifier)

Series PVR33 — MOSFET® Photovoltaic Relay

International
IOR Rectifier

Electrical Specifications ($-40^{\circ}\text{C} \leq T_A \leq +85^{\circ}\text{C}$ unless otherwise specified)

INPUT CHARACTERISTICS		Units
Minimum Control Current (see figure 1)		DC
For 20mA Continuous Load Current	2.0	mA @ 25°C
For 100mA Continuous Load Current	5.0	mA @ 25°C
For 20mA Continuous Load Current	5.0	mA @ 85°C
Minimum Turn-Off Current	10	μA(DC)
Minimum Turn-Off Voltage	0.6	V(DC)
Control Current Range (Caution: current limit input LED. See figure 6)	2.0 to 25	mA(DC)
Maximum Reverse Voltage	7.0	V(DC)

OUTPUT CHARACTERISTICS	PVR2300	PVR3300, PVR3301	Units
Operating Voltage Range	±200	±300	V _(peak)
Maximum Load Current 40°C (see figure 1)			
AC (A Connection)	180		mA (peak)
DC (B Connection)	200		mA(DC)
DC (C Connection)	260		mA(DC)
Response Time @ 25°C (see figure 7)			
Max. T _(on) @ 12mA Control, 100 mA Load, 100 VDC	150		μs
Max. T _(off) @ 12mA Control, 100 mA Load, 100 VDC	50		μs
Max. On-state Resistance 25°C (Pulsed) (fig. 2) 50 mA Load, 8mA Control			
AC (A Connection)	24		Ω
DC (B Connection)	12		Ω
DC (C Connection)	6		Ω
Min. Off-state Resistance 25°C @ 160 VDC PVR2300, PVR3300	10 ⁸		Ω
@ 240 VDC PVR3301	10 ¹⁰		Ω
Max. Thermal Offset Voltage @ 5.0mA Control	0.2		μvolts
Min. Off-State dv/dt	1000		V/μs
Output Capacitance (see figure 3)	12		pF @ 50VDC

GENERAL CHARACTERISTICS (PVR2300, PVR3300, PVR1301)		Units
Dielectric Strength: Input-Output	1500	V _{RMS}
Insulation Resistance: Input-Output @ 500V _{DC}	10 ⁹	Ω
Maximum Capacitance: Input-Output	1.0	pF
Max. Lead Soldering Temperature (1.6mm below seating plane for 10 sec)	260	°C
Ambient Temperature Range:		
Operating	-40 to +85	°C
Storage	-40 to +100	

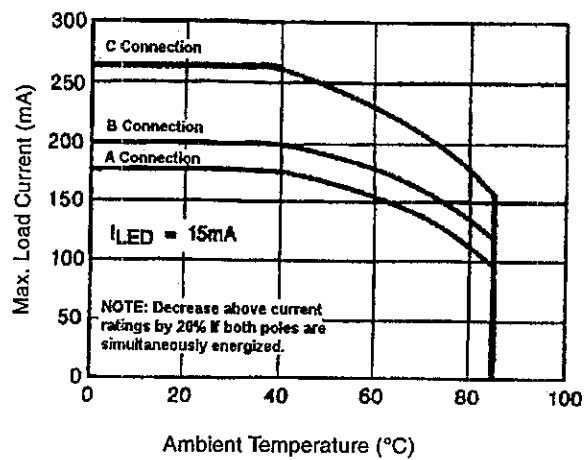


Figure 1. Current Derating Curve

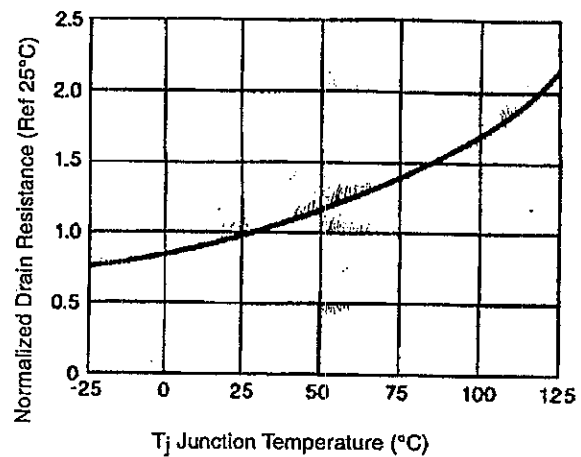


Figure 2. Typical Normalized On-Resistance

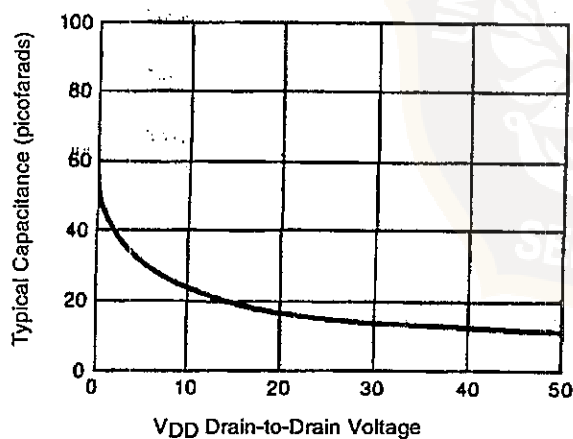


Figure 3. Typical Output Capacitance

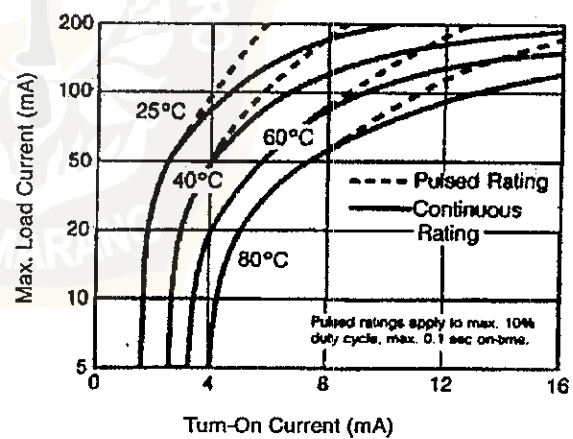


Figure 4. Minimum Control Current for Full Turn-On

Series PVR33 — BOSFET® Photovoltaic Relay

International
IOR Rectifier

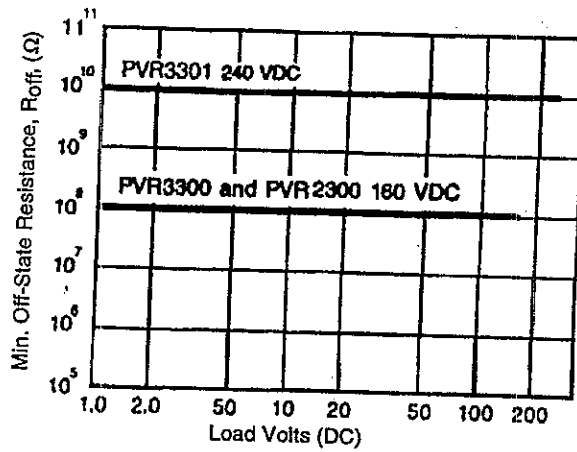


Figure 5. Off-State Resistance

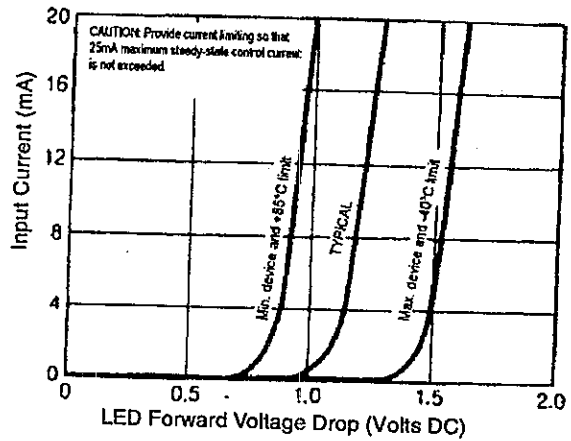


Figure 6. Input Characteristics (Current Controlled)

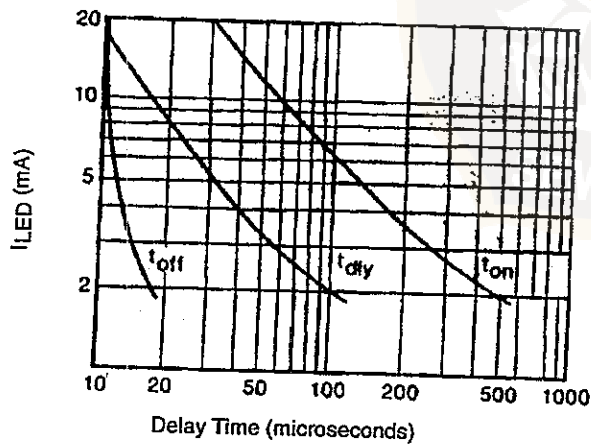


Figure 7. Typical Delay Times

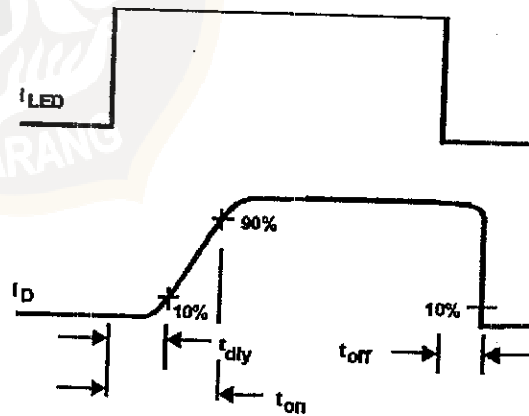
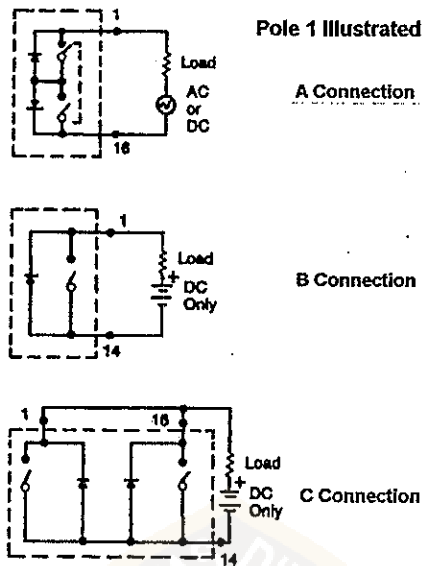
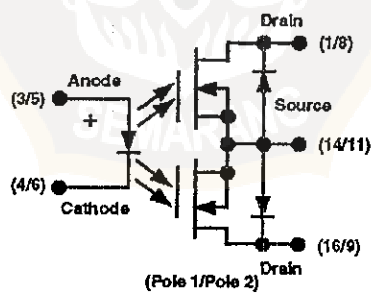


Figure 8. Delay Time Definitions

Wiring Diagram



Schematic Diagram

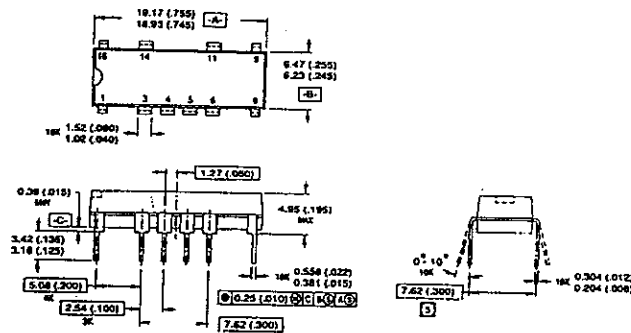


Series PVR33 — BOSFET® Photovoltaic Relay

International
IOR Rectifier

Case Outline

(Dimensions in inches (millimeters))



Mechanical Specifications:

Package: 16-pin DIP

Tolerances: .015 (.38) unless otherwise specified

Case Material: molded epoxy

International
IOR Rectifier

WORLD HEADQUARTERS: 233 Kansas St., El Segundo, California 90245, Tel: (310) 322 3331

EUROPEAN HEADQUARTERS: Hurst Green, Oxted, Surrey RH8 9BB, UK Tel: ++ 44 1883 713215

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IR ITALY: Via Liguria 49, 10071 Borgaro, Torino Tel: ++ 39 11 451 0111

IR FAR EAST: K&H Bldg., 2F, 3-30-4 Nishi-Ikeburo 3-Chome, Toshima-Ku, Tokyo, Japan 171 Tel: ++ 81 3 3983 0641

IR SOUTHEAST ASIA: 315 Outram Road, #10-02 Tan Boon Liat Building, Singapore 0316 Tel: ++ 65 221 8371

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Data and specifications subject to change without notice. 9/96

Lampiran 7

Tabel Permeabilitas Material (Mitchell, 1992)

Material	Permeabilitas (μ)
Udara/ vakum	$1,26 \times 10^{-6}$
Nikel	$6,28 \times 10^{-5}$
Cobalt	$5,56 \times 10^{-5}$
Cast iron	$1,1 \times 10^{-4}$
Machine steel	$5,65 \times 10^{-4}$
Transformer iron	$6,9 \times 10^{-3}$
Silikon iron	0,126
Permaloy	1,26
Superalloy	



Lampiran 8

Penurunan Persamaan Matematis

I. Induktansi timbal balik antara dua kumparan

Menurut definisi k_{12} pada persamaan 2.4 dan mengingat persamaan 2.2., didapatkan:

$$\phi_{12} = k_{12} \phi_{22} = k_{12} L_2 i_2$$

$$\phi_{12} = M i_2$$

yang berarti:

$$M = k_{12} L_2$$

Dengan jalan yang sama akan diperoleh

$$M = k_{21} L_1$$

Sehingga dengan demikian dapat dirumuskan induktansi timbal balik antara dua kumparan sebagai:

$$\begin{aligned} M &= \sqrt{k_{12} L_{12} \cdot k_{21} L_1} \\ &= k \sqrt{L_1 L_2} \end{aligned} \quad (2.5)$$

$$\text{dengan } k = \sqrt{k_{12} k_{21}}$$

II. Tenaga sistem kumpulan yang dialiri arus listrik

Tenaga yang dikandung di lingkaran arus ke j oleh arus i di kumpulan itu sendiri diberikan oleh

$$\begin{aligned}U_{ji} &= \int dU_{ji} = \int i_j d\phi_{ji} \\&= \int i_j L_{ji} di_j \\&= \frac{1}{2} L_{ji} i_j^2 \\&= \frac{1}{2} i_j \phi_{ji}\end{aligned}$$

Seandainya mula-mula tidak ada arus listrik di masing-masing lingkaran, lalu arus listrik i_1, i_2, i_3, \dots dst. dialirkan berurutan ke lingkaran ke 1, 2, 3, \dots dst. maka tenaga yang kemudian terdapat dalam sistem lingkaran-lingkaran arus listrik menjadi

$$U_j = i_j \phi_{j1} + i_j \phi_{j2} + \dots + \frac{1}{2} i_j \phi_{jj}$$

$$U = \sum_j U_j$$

$$L_{ji} = L_{ij} \text{ sehingga, } i_j \phi_{ji} = i_j L_{ji} i_i = i_i L_{ij} i_j = i_i \phi_{ij}$$

Tenaga sistem lingkaran-lingkaran arus listrik tersebut dapat ditulis sebagai

$$\begin{aligned}U &= \sum_j \frac{1}{2} i_j \phi_{jj} + \frac{1}{2} \sum_j \sum_{i \neq j} i_j \phi_{ji} \\&= \frac{1}{2} \sum_j \sum_i i_j \phi_{ji}\end{aligned} \tag{2.6}$$